Calculation of conducted EMI generated by single-ended primary inductance converter

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Abstract – This paper deals with the problem of conducted electromagnetic disturbances generated by a single-ended primary inductance converter (SEPIC) switching power supply for radar applications. In the proposed model the passive components are replaced by their high frequency (HF) equivalent models and the active elements by the interference sources. The six windings transformer, which is one of the passive elements of the switching power supply allows the adaptation of voltage levels and provides galvanic isolation between input and output. It will be modeled by: a simplified model and then by a model taking into account coupling between the leakage inductances. The accuracy of each model is established by comparing the simulation results of conducted electromagnetic interference (EMI) to measurement results.

Keywords: electromagnetic interference (EMI), emission, frequency domain analysis, measurement, power electronics.

I. Introduction

The increase of switching frequency in power converters allows reducing the volume of power supplies. However, this increase in frequency generates disturbances, mostly due to high \( \frac{di}{dt} \) loops and high \( \frac{dv}{dt} \) nodes in power stages, on the mains network. To meet the standards that define the limits of conducted disturbances supported by the network, it is highly recommended to quantify these disturbances allowing to have a pre-qualification of conducted emissions before design.

Numerical computation is an effective way of study the high frequency (HF) behavior of power converters structures in time and a frequency domain. It allows the designer to reduce the number of prototypes during the design phases. Moreover, the use of these tools allows a better understanding of electromagnetic phenomena in power converters and better system optimisation.

Time domain simulations offer good results for simple systems. However, for complex systems, simulations become very slow and discrepancies start occurring. Given the complexity of the studied power supply (multi-winding transformer, the presence of multiple filters, large number of components) and in order to avoid the draw backs of time-domain methods, a frequency-domain simulation has been chosen.

The modelling presented in this paper consists of: modeling of the active elements by interference sources (voltage), replace passive components such as capacitors, coils and resistors by their HF equivalent models, establish the equivalent diagram of the overall structure and calculate the conducted electromagnetic disturbances that can interfere with the mains network.

After presenting the studied power supply, this paper focuses on the calculation of disturbances in differential-mode and common-mode for two HF transformer models: the first one without leakage inductances coupling and the other with this coupling. The results are then compared with measurements for validation.

II. Studied switching power supply

The Fig 1 shows the classical diagram of a single-ended primary inductance converter (SEPIC). This converter lowers the voltage from 320 V (rectified mains voltage) to 56 V. Its switching frequency is 100 kHz and the transmitted power is 1350 W.

![Fig 1 SEPIC topology, including filters and rectifier](image)

In the studied structure:
- \( L_2 \) is replaced by a transformer to decrease the output voltage and ensure galvanic isolation.
- In order not to exceed the maximum current allowable by the diode D, a current division was adopted by using a multi-windings transformer multiplying the number of secondary windings by 4.
- The coil \( L_1 \) is placed on the same core as the transformer because it was found that their voltages have the same instantaneous values, and it allows a significant volume reduction.
- The switch SW is composed of three MOSFETs (MTW10N100E) put in parallel for two reasons: firstly, dividing the current through each MOSFET, and secondly, reducing the equivalent impedance value of the whole switch.

Such modification of the basic structure make it much more complex (fig 2) and prevent us from an easy EMC study.

Indeed, in addition to the items cited above, the converter features storage and filtering capacities: $C_{IN}$, $C_1$ et $C_2$, bridge rectifier, RC circuits protection at the diodes terminals and filters at the power supply entry.

III. Active component modeling

To analyze this power supply in frequency domain, both in differential and common modes, we replace non-linear and time dependent MOSFETs and diodes by [1]:

- a voltage source which is the voltage measured at its terminals VMOSFET (VDiode) (fig 3, fig 4)
- its parasitic inductances $L_D$, $L_S$ ($L_A$, $L_K$) given by the manufacturers;
- and a dynamic impedance identified by measurement with behave as: an inductance during conduction ($L_{Dyn}$), zero impedance while switching and capacitance while blocking ($C_{Dyn}$) as identified by the impedance measurement.

Over a switching period T, we find that the measured voltage can be decomposed into several mathematical functions (TABLE I). The model then consists of replacing the voltage source representing the MOSFETS (Diodes) by mathematical equations that reproduce the same waveforms. These equations will be transposed later in the frequency domain (using Laplace transforms) as described in TABLE II.

![Fig 2 Studied SEPIC](image-url)
Fig 3 Equivalent model for MOSFET (diode) while: (a) switching, (b) blocking and (c) conducting

TABLE I
FORMULATION OF VOLTAGE WAVEFORM AT THE TRANSISTOR TERMINALS IN RELATION WITH ITS STATE

<table>
<thead>
<tr>
<th>Voltage wave at the transistor terminals</th>
<th>Analytic equations</th>
</tr>
</thead>
<tbody>
<tr>
<td>In the time interval ([T_0 - T_f])</td>
<td>(V_{\text{rampes-OFF}} = A_1 U(t-T_0))</td>
</tr>
<tr>
<td>(T_f - T_1)</td>
<td>(V_{\text{rampes-OFF}} = \frac{A_2 - A_1}{T_f - T_0} U(t-T_0))</td>
</tr>
<tr>
<td>(T_f - T_1)</td>
<td>(V_{\text{OFF1}} = A_2 U(t-T_f))</td>
</tr>
<tr>
<td>(T_1 - T_f)</td>
<td>(V_{\text{OFF2}} = A_2 U(t-T_f))</td>
</tr>
</tbody>
</table>

\(A_1 = 600\) \(V\) \(K_1 = 0.625\times 10^{-6}\) \(B = 2\times 2.10^{10}\) \(T_{\text{max}} = T_r - T_f\)

\(V_{\text{rampes-ON}} = A_3 U(t-T_f)\)

\(V_{\text{ON}} = A_4 U(t-T_f)\)

\(T_r = 0.8\mu s\)

\(T_f = 3.2\mu s\)

\(A_1 = 600\) \(V\)

\(A_2 = 312\) \(V\)

\(T_{\text{max}} = T_r - T_f\)

\(K_1 = 0.625\times 10^{-6}\)

\(B = 2\times 2.10^{10}\)

Fig 4 Measured voltage waveform of the transistor.

TABLE II
FORMULATION OF VOLTAGE WAVEFORMS IN FREQUENCY DOMAIN

\(V_{\text{rampes-OFF}} = \frac{1}{p} (A_1 e^{-T_0 \cdot p} - A_2 e^{-T_r \cdot p}) + \frac{A_2 - A_1}{T_r - T_0} \frac{1}{p^2} (e^{-T_0 \cdot p} - e^{-T_r \cdot p})\)

\(V_{\text{rampes-ON}} = \frac{A_3}{T_f - T_0} \frac{1}{p^2} (e^{-T_0 \cdot p} - e^{-T_f \cdot p})\)

\(V_{\text{OFF1}} = \frac{A_2}{p} (e^{-T_f \cdot p} - e^{-T_1 \cdot p})\)
IV. Capacitor and resistor model

In High Frequency, the passive components have frequency-dependent behavior [2]-[3]-[4]. The HF model is obtained by impedance measurements in the frequency range of 100 kHz to 30 MHz.

At the end of each measurement, an equivalent electrical model combining inductance, resistances and capacities is established (fig 5). This model needs parameters identification, using numerical methods.

![Equivalent circuit model of capacitor (a) and resistor (b)](image)

To validate the calculation, for example, a comparative study between the measured impedance of the filter capacitor (using a HP 4294 impedance analyzer) and a computed value (from the equivalent circuit diagram) was performed. We note a good agreement between measurement and calculation, with validates the model of this capacitor.

![Impedance comparison](image)

V. Transformer model without leakage inductors couplers

The studied transformer converts a voltage from 320 V to 56 V and provides galvanic isolation between its input and outputs.

It consists of (Fig 7):

- a transformer T1-4, containing a primary winding 3-4 and four secondary windings;
- and a storage coil L1-2, placed on the same transformer core.

These two elements listed above have been modeled separately. The coupling between the coil L1-2 and the transformer primary winding has been modeled through their mutual impedance.

![SEPIC Transformer](image)

V.1 Inductor L1-2 model

The inductor 1-2 is modeled by:

- the impedance \( Z_{L1-2} \) measured across its terminals,
- and its mutual impedance \( Z_{M1-2} \) measured across the terminals of both 1-2 and 3-4 parallel coils terminals.

![Inductor L1-2 model](image)

Fig 8 shows equivalent electrical circuits of impedance \( Z_{L1-2} \) and mutual impedance \( Z_{M1-2} \). The choice of these circuits is confirmed by comparisons between calculated impedances and measurements (Fig 9, Fig 10).
The HF equivalent circuit of the transformer consists of [5]:
- a magnetic part representing the currents circulation
- and a capacitive part allowing the circulation of parasitic currents to be dealt with later in C)
The resulting circuits are composed of inductive elements and couplers allowing the representation of electric and magnetic links existing between the different windings. The extraction of these elements is based on measurements using the impedance analyzer HP 4294 (40 Hz-110 MHz).

The equivalent circuit of the transformer T1-4 without parasitic capacitances is represented by (Fig 11):
- 5 inductors: magnetising inductor $L_m$, and secondary leakage inductances $L_{f1}$, $L_{f2}$, $L_{f3}$ and $L_{f4}$
- and 4 principal couplers ($n_{1:2}$, $n_{1:3}$, $n_{1:4}$ and $n_{1:5}$)

The inductances and principal couplers are calculated directly from impedance measurements (TABLE III). Nine parameters need to be identified, which requires nine independent impedance measurements ($Z_{m1}$, ..., $Z_{m9}$), include:

<table>
<thead>
<tr>
<th>TABLE III</th>
<th>Inductances Measurement Configurations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Measure</td>
<td>Inductors and couplers</td>
</tr>
<tr>
<td>$Z_{m1}$</td>
<td>$L_m = \frac{Z_{m1}}{2\pi f}$</td>
</tr>
<tr>
<td>$Z_{m2}$</td>
<td>$L_{f1} = \frac{Z_{m2}}{2\pi f}$</td>
</tr>
</tbody>
</table>
### Transformer T1-4 model with parasitic capacitances

To take into account the HF behavior, we now integrate the parasitic capacitances (fig 13)

- windings: \(C_1, C_6, C_7, C_8\) and \(C_9\);
- and inter-windings: \(C_2, C_3, C_4, C_5, C_{10}, C_{11}\) and \(C_{12}\)

The schematics become more complex and more elements need to be identified.

**TABLE IV**

<table>
<thead>
<tr>
<th>Parasitic capacitances</th>
<th>Measurement configurations</th>
</tr>
</thead>
<tbody>
<tr>
<td>(C_1 + C_2 + C_3 + C_4 + C_5)</td>
<td>(\frac{1}{Z_{m1.2\varphi}}) (\varphi = \pi / 2)</td>
</tr>
<tr>
<td>(C_2 + C_3 + C_4 + C_5 + C_6 + C_7 + C_8 + C_9)</td>
<td>(\frac{1}{Z_{m2.2\varphi}}) (\varphi = \pi / 2)</td>
</tr>
<tr>
<td>(C_2 + C_6 + C_{10})</td>
<td>(\frac{1}{Z_{m3.2\varphi}}) (\varphi = \pi / 2)</td>
</tr>
</tbody>
</table>

These capacitances are identified from the system of equations obtained by impedance measurements (TABLE IV). To avoid a second order system, measurements are done by short-circuiting the largest possible number of capacitances.

The other parameters representing magnetic coupling (\(L_{f1}, L_{f2}, L_{f3}, L_{f4}, n_{1:2}, n_{1:3}, n_{1:4}\) and \(n_{1:5}\)) are calculated from impedance measurements cited in TABLE III.
The example of the first measurement $Z_{m1}$ (TABLE IV) is given in Fig 14. The value of parasitic capacitance is deduced at:

$$f = 13.65 \text{ MHz}, \quad pF = 369 \mu F$$

This value is the sum of parasitic capacitances which gives the first equation of the system:

$$C_{m1} = C_1 + C_2 + C_3 + C_4 + C_5 = 369 \mu F \quad (1)$$

With the 11 other measurements ($Z_{m2}, \ldots, Z_{m12}$), we obtain a system of 11 equations with 11 unknowns. The values of parasitic capacitances are obtained by solving the equations system.

VI. Measure and calculation of disturbances in differential-mode and common-mode

VI.1 Spectrum measurements

We distinguish two classes of conducted disturbances:
- those of common-mode (CM), which are spread mainly between live, neutral and earth via parasitic capacitances;
- and the differential-mode (DM), which spreads between live and neutral.

In this study, measurements were made using a clamp-on ammeter F 52 (100 kHz-500 MHz).

The configuration shown in Fig 15 measures the CM current directly in dBμV. The DM current, it is calculated by dividing the measured current by two.

$$I_{dBμV} = 27.958 + I_{dBμA} + Z_{pince} \quad (2)$$
Where:

- \( I_{\text{dB}\mu V} \) = disturbance spectrum;
- \( I_{\text{dB}\mu A} \) = disturbance spectrum observed on the spectrum analyzer;
- \( Z_{\text{pince}} \) = clamp impedance.

In Fig 16 we show the CM and DM measured disturbances spectrums.

**VI.2 Calculation and comparison**

For convergence reasons and to save simulation time, we have preferred calculating the disturbances in the frequency domain.

After establishing the complete power supply equivalent circuit, by replacing all components by their models, we obtain a mesh called harmonic model (fig 17), which is then transposed in the form of a square matrix (3) regrouping the equations from Kirchhoff laws.

\[
[Z][I]=[V]
\]

Where:
- \([Z]\) = system impedance matrix \([\Omega]\)
- \([I]\) = vector of unknown currents \([A]\)
- \([V]\) = vector of excitation sources \([V]\)

The following step consists of estimating the DM and CM currents to be estimated solving the matrix system using MATLAB. Indeed, the current vector \([I]\) especially contains \( i_{\text{MC}}, i_1, i_2 \) currents. The DM current is then calculated as a function of \( i_1 \) and \( i_2 \) by:

\[
I_{\text{md}} = \frac{(I_1 + I_2)}{2}
\]

Multiplying the current by 50 \(\Omega\), we find the value of electromagnetic disturbances in dB\(\mu V\). Fig 18 and Fig 19 show a comparison between computed spectral envelope and measured spectrum, in differential-mode and common-mode respectively.
For differential-mode calculation, we note a good agreement between calculated spectral envelope and measured spectrum disturbances. However, for common-mode calculation, we note a discrepancy. That is why a second model taking into account the coupling of transformer $T_{1.5}$ leakage inductances was adopted.

**VII. Transformer model with leakage inductances coupling and validation**

In this model, coupling from leakage inductances is taken into account in addition to inductors, main coupling and parasitic capacitance. The equivalent diagram of this model (fig 20) then contains: 5 inductances ($L_{i1}$, $L_{i2}$, $L_{i3}$ and $L_{i4}$), 4 principal couplers ($n_{1.2}$, $n_{1.3}$, $n_{1.4}$ and $n_{1.5}$), 3 couplers for the rank 4 leakage transformer ($n_{2.3}$, $n_{2.4}$ and $n_{2.5}$), 2 couplers for the rank 3 leakage transformer ($n_{3.4}$ and $n_{3.5}$) and 1 coupler for the rank 2 leakage transformer ($n_{4.5}$).

The 5 inductances ($L_m$, $L_{i1}$, $L_{i2}$, $L_{i3}$ and $L_{i4}$) and the parasitic capacitances ($C_1$...$C_{12}$) are the same as calculated in TABLE III and TABLE IV. The ten other parameters ($n_{1.2}$, $n_{1.3}$, $n_{1.4}$, $n_{1.5}$, $n_{2.3}$, $n_{2.4}$, $n_{2.5}$, $n_{3.4}$, $n_{3.5}$ and $n_{4.5}$) are calculated from the equations obtained by impedance measurements defined in TABLE V.

**TABLE V**

<table>
<thead>
<tr>
<th>Meas</th>
<th>Coupler</th>
<th>view of the winding</th>
<th>With</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z_{m6}$</td>
<td>$L_{f1} + n_{1.2}^2 + L_m = \frac{Z_{m6}}{2\pi} \theta = \pi / 2$</td>
<td>8 to 12</td>
<td>$i_1 = i_2 = i_4 = i_5 = 0$</td>
</tr>
<tr>
<td>$Z_{m7}$</td>
<td>$L_{f2} + n_{3.3}^2 + n_{1.3}^2 + L_m = \frac{Z_{m7}}{2\pi} \theta = \pi / 2$</td>
<td>7 to 11</td>
<td>$i_1 = i_2 \neq i_4 = i_5 = 0$</td>
</tr>
<tr>
<td>$Z_{m8}$</td>
<td>$L_{f3} + n_{2.4}^2 + n_{1.4}^2 + L_{f2} + n_{3.4}^2 + L_m = \frac{Z_{m8}}{2\pi} \theta = \pi / 2$</td>
<td>5 to 9</td>
<td>$i_1 = i_2 = i_3 = i_5 = 0$</td>
</tr>
<tr>
<td>$Z_{m9}$</td>
<td>$L_{f4} + n_{3.5}^2 + L_{f1} + n_{3.5}^2 + L_{f2} + n_{4.5}^2 + L_{f3} + n_{2.5}^2 + L_m = \frac{Z_{m9}}{2\pi} \theta = \pi / 2$</td>
<td>6 to 10</td>
<td>$i_1 = i_2 = i_3 = i_4 = 0$</td>
</tr>
<tr>
<td>$Z_{m10}$</td>
<td>$L_{f1} - \frac{L_{f2}}{n_{3.3}} - \frac{L_{f1}}{n_{2.3}} = \frac{Z_{m10}}{2\pi} \theta = \pi / 2$</td>
<td>8 to 12</td>
<td>$i_4 = i_5 = 0$ and $v_1 = v_3 = 0$</td>
</tr>
<tr>
<td>$Z_{m11}$</td>
<td>$L_{f2} - \frac{L_{f3} + n_{2.4}.L_{f1}}{n_{2.4}^2} - \frac{L_{f2} + L_{f3} + n_{1.4}.L_{f1}}{n_{3.4}^2} = \frac{Z_{m11}}{2\pi} \theta = \pi / 2$</td>
<td>7 to 11</td>
<td>$i_2 = i_5 = 0$ and $v_1 = v_4 = 0$</td>
</tr>
<tr>
<td>$Z_{m12}$</td>
<td>$L_{f2} + n_{2.4}^2 + L_{f1} + n_{2.4}^2 + L_{f2} + L_{f3} + n_{3.5}^2 + L_{f2} = \frac{Z_{m12}}{2\pi} \theta = \pi / 2$</td>
<td>5 to 9</td>
<td>$i_2 = i_3 = 0$ and $v_1 = v_5 = 0$</td>
</tr>
</tbody>
</table>
The results (Fig 21, Fig 22) show a good agreement between measurements and calculations, of electromagnetic disturbances in CM as in DM; thus validating the HF model with leakage inductances.

### References


Authors’ information

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